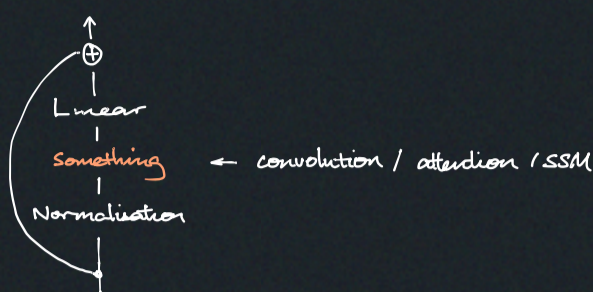


# Lec 16 Long Seq Modelling

Deep sequence models very useful

Sequence model:  $\text{seq} \xrightarrow{f_{\theta}(\cdot)} \text{seq}$

RNN, CNN, Neural ODEs, Attention



## # Baselines

- RNN — recurrence cells
- + inherently causal
  - slow training
  - vanishing gradient

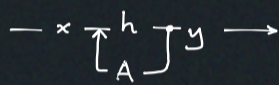
Attention

- + parallelisable
- quadratic time training
  - ↳ finite context window

→ Selective State Spaces

- + parallel, fast, linear
- + long context
- + performance

## # SSM



signal processing  
continuous, diff EQ  
like RNN with continuous time,  
big hidden state,  
no activation,  
linear

$$h'(t) = \overset{\square}{A} h(t) + \overset{\parallel}{B} x(t)$$

↑ state transition                      ↑ transform input

$$y(t) = \overset{\square}{C} h(t) + \overset{\square}{D} x(t)$$

↑ project back to 1D                      ↑ skip connection

Biased for continuous data, less good for text

▷ Discretised

$$h = \bar{A}h + \bar{B}x$$

$$y = \bar{C}h + \bar{D}x$$

\* Issues

- no parallelisation along seq length
- large hidden (expensive)
- harder to train, given known future

▷ Convolution version of SSM

Equivalent to convolution

$$y(t) = x(t) * K(t)$$

↑ convolution kernel defined by A, B, C, D

+ Fast fourier transform, near linear time

## # SSSM

Linear Time Invariant — params invariant through time

SSSM — State Space Seq Model

SSSSM — Structured State Space Seq Model

Things viewed as SSM:

- RNN → state is one fixed-sized vec  
efficient, maybe too strong of compression on history
- Attention → state is cache of entire history  
attend to all past key & value  
good history, bad performance

## # Better model

Compress, selectively remember relevant information

Doing the selection: parametrise update func on current input

Make efficient: need to tailor to GPU hardware