

Lec 1

Philosophy of class

1. Computation is naturally functional
2. Programming is explanatory process

Imperative: things have states that change
 $x := 5$

Functional: evaluation
 $3+4 \rightarrow 7$

→ Problem statement

- Think mathematical
 - ↳ Invariants
 - ↳ Specifications
 - ↳ Proof of correctness

Parallelism

- Work - total num of operations running on one process sequentially
- Span - running time on ∞ processors. longest / critical path length

Expressions

$(3+4)*2$
→ $7*2$
→ 14

Num of steps
 $(3+4)*(1+1)$
→ $7*(1+1)$
→ $7*2$
→ 14

Parallel

$(3+4)*(1+1)$
→ $7*2$
→ 14

"hello" ^ "world"
→ "hello world"

$1 + \text{"world"}$
⚠ Type error ← type coercion
bad idea?

Type checking!

"Certainly the most important concept in ML."

* ML type checks first. Only compiles when passes

Eg.

$(3+4) * 1 : \text{int}$
"w" ^ "d" : string] "well-typed"
 $1 + \text{"world"}$ no type, "ill typed" ← Not even worth talking about.
Don't evaluate
They don't make sense. Don't consider

Type := prediction of the form of future value, if we ever get one.

* Every well-formed expression:
- Has a type
- May have a value
- May cause an effect ← e.g. print

$e : t$
 $e \rightarrow v$
T
may evaluate to value

We write:

$(3+4) * (1+1) : \text{int}$
→ 14

Some types

Base types: int char
real string
bool ...

Type check and run

$e_1 + e_2$ int if $e_1 : \text{int}$ and $e_2 : \text{int}$

* We do typing "statically"

- but we run to get value, that's "dynamic"

Composite : products
functions
datatypes ← will define these later
:

Evaluation rules

$e_1 + e_2 \Rightarrow e_1' + e_2$ if $e_1 \Rightarrow e_1'$ ↖ one step of evaluation
 $n_1 + e_2 \Rightarrow n_1 + e_2'$ if $e_2 \Rightarrow e_2'$ ↖ evaluated
 $n_1 + n_2 \Rightarrow n$ where $n = e_1 + e_2$ ↖ final evaluation
 $e \Rightarrow v$ if $e \Rightarrow v$ and v is value ↖ reduce as much as possible.

Ex. $5 \text{ div } 0$ all good
type check: $5 \text{ div } 0 : \text{int}$
run: Div exception
Uhoh

Extensional Equivalence (eeq)

$1 + 2 \hookrightarrow 3$ $0 + 3 \hookrightarrow 3$
They eval. to same value, they are eeq!
Write $1 + 2 \cong 0 + 3$

Def of \cong is type-dependent.

For most types $e_1 \cong e_2$ if:

- they have same type
 - they eval to same value
- OR
- they raise same exception
- OR
- they both loop

⚠ function isn't like this

For functions, eeq if:

- same type
- eeq result given eeq argument.

Product type

name: $t_1 * t_2$

value: (v_1, v_2)

expressions: (e_1, e_2)

$(\#_1, \#_2)$

↖ some deprecated thing

typing rule: $(e_1, e_2) : t_1 * t_2$ if $e_1 : t_1$ and $e_2 : t_2$
evaluation: left to right

Ex.

(5 div 0, 2+1) : int * int
↳

(8 + "hello", false) ill typed : C
Don't even eval.

(2, (true, "a")) : int * (bool * string)

↳ this one more memory efficient ↗ Not same
↳ (2, true, "a") : int * bool * string

Functions

(* square : int → int
REQ : true
ENS : square (x) evals to x*x
)
fun square (x : int) : int = x

Binding

Indicates "I bound to x"

val x : int = 1 [1/x]
val y : int = x + 1 [2/y]
val x : int = 10 [10/x]
val z : int = 2 * x [20/z]
↳ looks for most recent binding

We don't "change" binding -
Old one "shadowed"

Local binding

val x : int = 1 [1/x]
let
 val x : int = 10 [10/x] ← This is one expression
 and
 x + 10 ↳ 20.
end
val y : int = x [1/y]