

## Lec 7

## Semantic Analysis

Recall IR tree & type judgement

Type judgement :  $\Gamma \vdash e : \tau$

context  $\Gamma ::= \cdot \mid \Gamma, x : \tau$

Rules  $\frac{\Gamma(x) = \tau}{\Gamma \vdash x : \tau}$      $\frac{\Gamma \vdash e_1 : \text{int} \quad \Gamma \vdash e_2 : \text{int}}{\Gamma \vdash e_1 + e_2 : \text{int}}$

### # Type Checking

assign ( $x, x+5$ ) requires :  $x : \text{int}$  (if  $x$  initialised) initial checking can be  
indep from type checking

Type of statement — have to consider side effect & returns

write  $\Gamma \vdash s : [\tau]$

statement      return type of func

"In context  $\Gamma$ ,  $s$  is well-typed and all args of  
returns have type  $\tau$ "

return ( $s$ ) requires : the func returns int

{

return ( $s$ ) ;

return (true) ; ← bad, even if already returned

}

$\frac{\Gamma \vdash e : \tau}{\Gamma \vdash \text{return}(e) : [\tau]}$      $\frac{\Gamma \vdash s_1 : [\tau] \quad \Gamma \vdash s_2 : [\tau]}{\Gamma \vdash \text{seq}(s_1, s_2) : [\tau]}$  ← no decl to share btwn  $s_1$  &  $s_2$

$\frac{\Gamma \vdash e : \tau' \quad \Gamma(x) : \tau'}{\Gamma \vdash \text{assign}(x, e) : [\tau]}$      $\frac{\Gamma, x : \tau' \vdash s : [\tau]}{\Gamma \vdash \text{decl}(x, \tau', s) : [\tau]}$

$\frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash s : [\tau]}{\Gamma \vdash \text{while}(e, s) : [\tau]}$      $\frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash s_1 : [\tau] \quad \Gamma \vdash s_2 : [\tau]}{\Gamma \vdash \text{if}(e, s_1, s_2) : [\tau]}$

### # Implementing These — Modes of Judgements

chk-exp : context  $\rightarrow$  exp  $\rightarrow$  type  $\rightarrow$  bool ?    Nope, since we might not have concrete type as input yet

syn-exp : context  $\rightarrow$  exp  $\rightarrow$  type

chk-stmt : context  $\rightarrow$  stmt  $\rightarrow$  type  $\rightarrow$  unit  
if not type check just raise exns

### # Initialisation Checking

Option 1: Use liveness, using these judgements

↑ given in language specs

use ( $e, x$ )     $x$  used in  $e$

def ( $s, x$ )     $s$  defined in  $s$

live ( $s, x$ )     $x$  live in  $s$

init ( $s$ )    all vars in  $s$  initialised

$$\frac{\neg \text{live}(s, x) \quad \text{init}(s)}{\text{init}(\text{decl}(x, \tau, s))}$$

Option 2: Alt judgements

$$\frac{\begin{array}{c} \gamma \delta \vdash s \Rightarrow \delta' \\ \parallel \quad \parallel \\ \text{initialised before } s \\ \text{declared before } s \end{array} \quad \begin{array}{c} \text{statement} \\ \parallel \\ \text{sets} \\ \parallel \\ \text{initialised after } s \end{array}}{\gamma \delta \vdash \text{assign}(x, e) \Rightarrow \delta \cup \{x\}}$$

$\delta \vdash e$   
 $e$  uses only vars initialised in  $\delta$

$$\frac{\gamma \delta \vdash s_1 \Rightarrow \delta_1 \quad \gamma \delta \vdash s_2 \Rightarrow \delta_2}{\gamma \delta \vdash \text{seq}(s_1, s_2) \Rightarrow \delta_2}$$

$$\frac{\delta \vdash e}{\gamma \delta \vdash \text{return}(e) \Rightarrow \delta}$$

### # Lexing — first pass to identify tokens

In: string source code

Out: token stream

int x ;                    TYPE (int)

// init                    VAR(x)

x = n;                    SEMI

EQ

VAR(n)

SEMI

Lexer spec

1.  $\Sigma = \{0, \dots, 9, a, \dots, z, (, ), \dots\}$

2. Mapping  $\Sigma^* \rightarrow \text{TokenType}$

L { TYPE, VAR, SEMI, ... }

usually by regex

Problem: mapping overlap, eg. if  $\rightarrow$  IF or Ident(if)

$\rightarrow$  Longest match first

$\rightarrow$  If same len, take first one in table

3

Execution: generate finite automata, run it, backtrack to last accept state