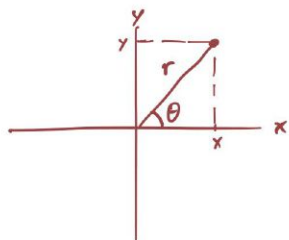


## Lec 18 Cylindrical & Cylindrical coord

### # Recall polar coord



$$r = \sqrt{x^2 + y^2}$$

$$\tan \theta = \frac{y}{x}$$

↑  
multiple soln.  
choose according to  
signs of x and y.

$$x = r \cos \theta$$

$$y = r \sin \theta$$

$$r = 3 \sin \theta \dots y = r \sin \theta$$

$$\Rightarrow \frac{r}{y} = \frac{3}{r} \Rightarrow r^2 = 3y$$

...  $\Rightarrow$  equation in x, y

### # Cylindrical coord

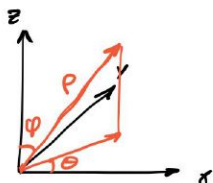
\*  $(x, y, z) \rightarrow (r, \theta, z)$  i.e. the  $z=0$  plane is polar.

$$r = z \Rightarrow \sqrt{x^2 + y^2} = z$$

$$r^2 + z^2 = 9 \Rightarrow x^2 + y^2 + z^2 = 9$$

### # Spherical coord

$(\rho, \theta, \varphi)$



$$\tan \theta = \frac{y}{x}$$

$$\cos \varphi = \frac{z}{\rho}$$

$$\rho = \sqrt{x^2 + y^2 + z^2}$$